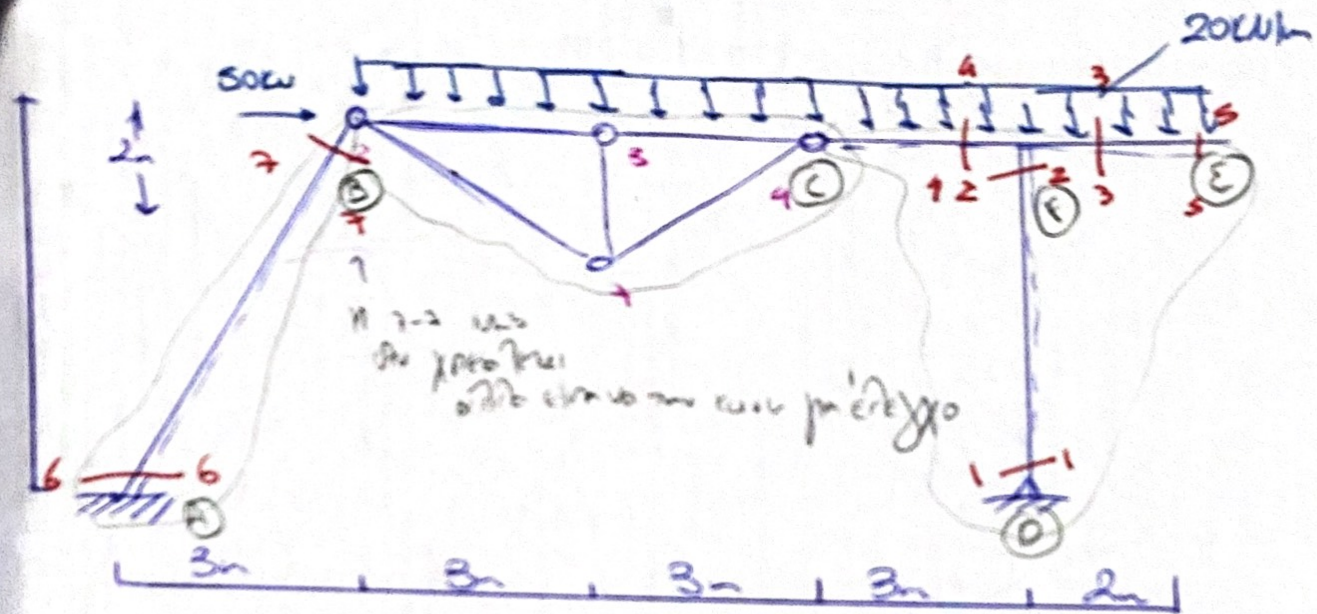
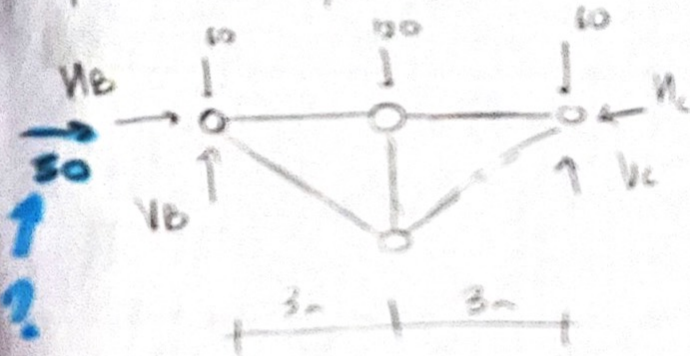




$$q l / 2 = 20 \times 6 / 2 = 60 \text{ kN}$$

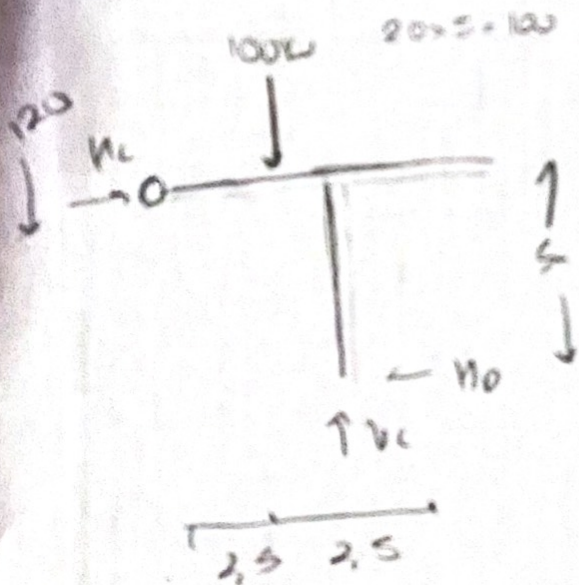


$$\sum F_x = 0 \Rightarrow 50 + H_B = H_C$$

$$\sum F_y = 0 \Rightarrow 60 + 120 + 60 = V_B + V_C \Rightarrow V_B + V_C = 240 \text{ kN}$$

$$\sum M_{B \rightarrow C} = (20 \times 3) + (60 \times 6) = 6V_C \Rightarrow V_C = 120 \text{ kN}$$

$$\text{Αρα } V_B = 120 \text{ kN}$$



$$\sum F_y = 0 \Rightarrow 120 + 100 = V_C \Rightarrow V_C = 220 \text{ kN}$$

$$\sum F_x = 0 \Rightarrow H_C = H_D$$

$$\sum M_{C \rightarrow D} = (-100 \times 2.5) + (3 \times 220)$$

$$- 5H_D = 0 \Rightarrow -250 + 660 - 5H_D = 0$$

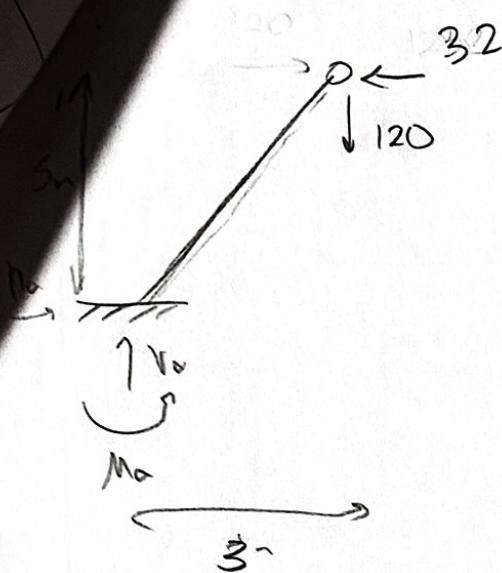
$$\Rightarrow 410 - 5H_D = 0 \Rightarrow H_D = 82 \text{ kN}$$

$$\text{Αρα } H_C = 82 \text{ kN}$$

$$H_B = 32 \text{ kN} \quad (32 + H_D = 82)$$

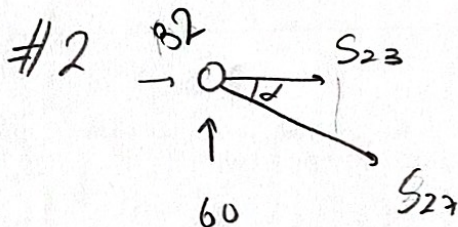
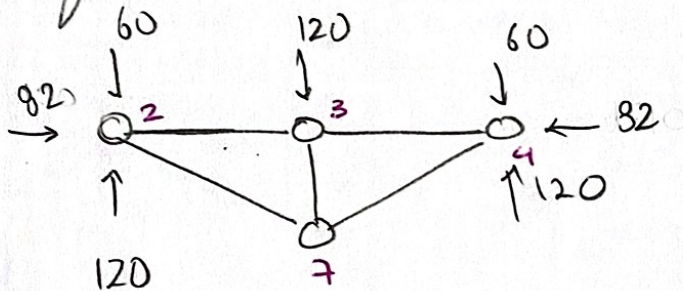
Ανswers: 1) OK το σύστημα

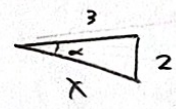
2) ως περσόνια λείπει



$$\begin{aligned}\sum F_x = 0 &\Rightarrow H_a = 32 \text{ kN} \\ \sum F_y = 0 &\Rightarrow V_a = 120 \text{ kN} \\ \sum M_A = 0 &\Rightarrow M_a + (32 \times 5) - (120 \times 3) \\ &\Rightarrow M_a = +200 \text{ kNm}\end{aligned}$$

Ma to dirimada.





$$\begin{aligned}x^2 &= 2^2 + 3^2 \\ \Rightarrow x &= 3,606\end{aligned}$$

$$\sin \alpha = \frac{2}{3,606} = 0,555$$

$$\cos \alpha = \frac{3}{3,606} = 0,832$$

$$\sum F_x = 0 \Rightarrow 82 + S_{23} + S_{27} \cos \alpha = 0$$

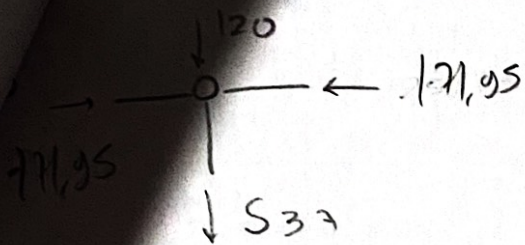
$$\sum F_y = 0 \Rightarrow 60 = S_{27} \sin \alpha \Rightarrow S_{27} = \frac{60}{0,555} = S_{27} = 108,11 \text{ kN}$$

$$\text{Ap: } 82 + S_{23} + 108,11 \times 0,832 = 0$$

$$\Rightarrow 82 + S_{23} + 89,95 = 0 \Rightarrow S_{23} = -171,95 \text{ kN}$$

#4 avtoraxa Agor avtoraxus

$$S_{43} = -171,95 \text{ kN} \quad \text{K} \quad S_{47} = 108,11 \text{ kN}$$



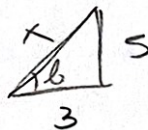
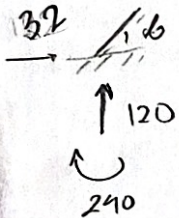
$$\sum F_x = 0 \checkmark$$

$$\sum F_y = 0 \Rightarrow 537 - 120 = 417$$

Μένος	Εφελκυσμός	Θάψη
2-3		77,95
3-4		77,95
2-7	109,11	
4-7	109,11	
3-7		120

70 ΜΕΣ

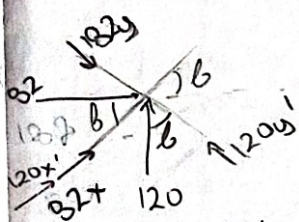
6-6



$$x^2 = 5^2 + 3^2 = x = 5,931$$

$$\cos b = \frac{3}{5,931} = 0,514$$

$$\sin b = \frac{4}{5,931} = 0,674$$



$$32_y = 32 \times \sin b = 21,42 \text{ kN}$$

$$32_x = 32 \times \cos b = 16,45 \text{ kN}$$

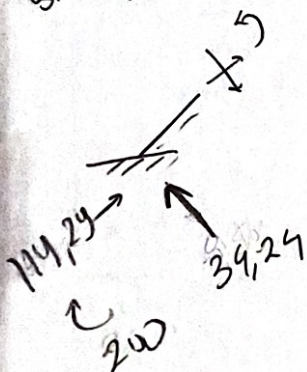
$$120_y' = 120 \times \cos b = 61,68 \text{ kN}$$

$$120_x' = 120 \times \sin b = 102,34 \text{ kN}$$

$$Q^A = +34,24 \text{ kN}$$

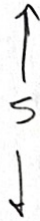
$$N^A = -119,29 \text{ kN}$$

$$M^A = +200 \text{ kNm}$$



$$Q_B^L = +34,24 \text{ kN}$$

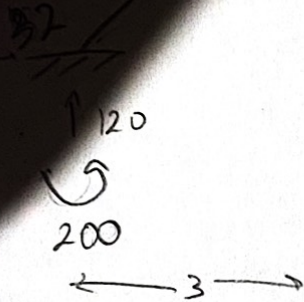
$$N_B^L = -119,29 \text{ kN}$$



$$M_B^L + 200 - (120 \times 3) + (32 \times 5) = 0$$

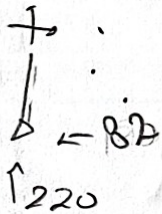
$$M_B^L + 200 - 360 + 160 = 0$$

$$\Rightarrow M_B^L = 0 \checkmark$$



1-1

$$M_D = 0, N_D = -220, Q_D = +82$$

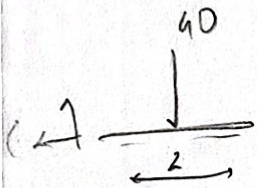


3-3

C F =

$$M_E = 0, Q_E = 0, N_E = 0$$

3-3



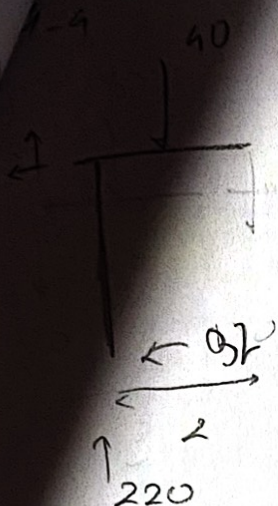
$$M_F^S = -40, Q_F^S = 40, N_F^S = 0$$

2-2



$$N_F^L = -220, Q_F^L = +82$$

$$M_F^L = +82 \times 5 = 410 \text{ kNm}$$



$$N_F^L = -32 \text{ kN}$$

$$Q_F^L = -120 \text{ kN}$$

$$M_F^L = (-32 \times 5) - (40 \times 1) = -160 \text{ kNm}$$

M-Q-N

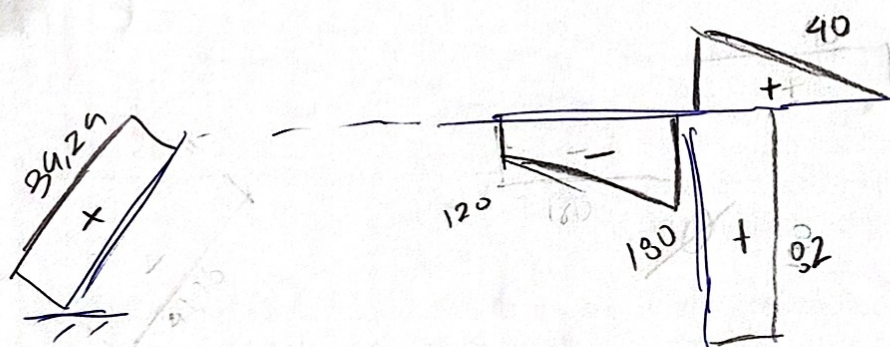
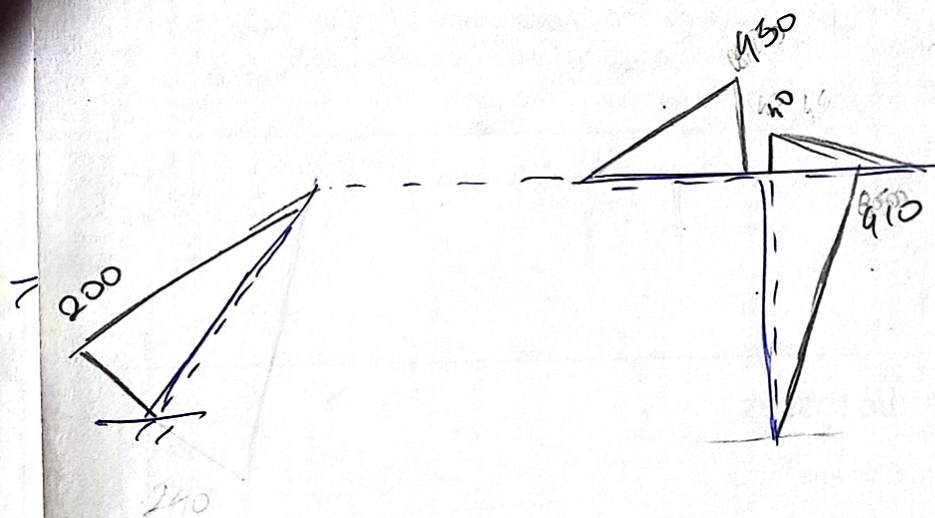
$$N = -32$$

$$Q = -120$$

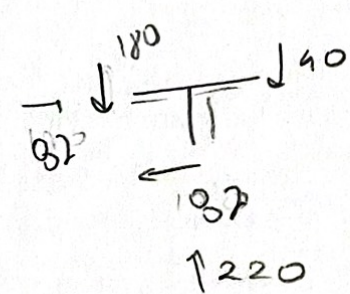
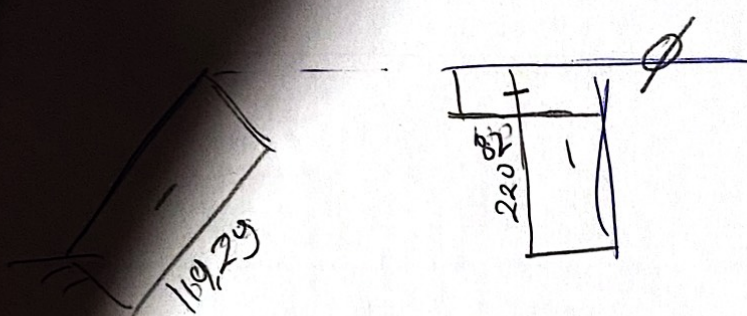
$$M = (120 \times 5) + (40 \times 1) = 620$$

M [kNm]

$$\frac{620}{5} = 124$$

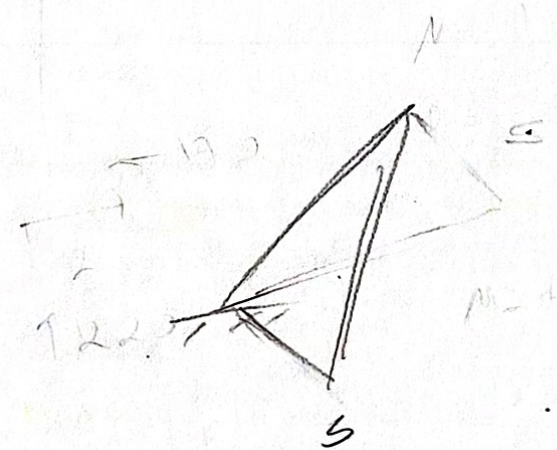
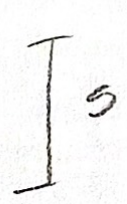
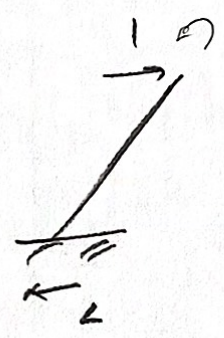
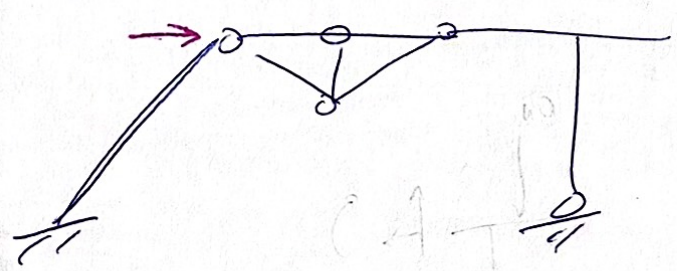


Q [kN]



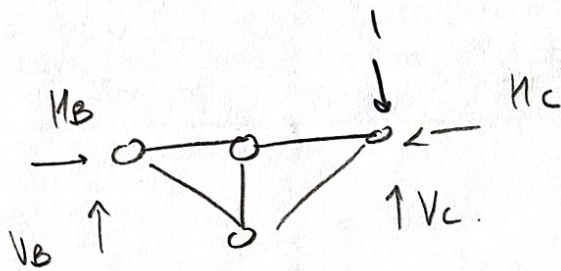
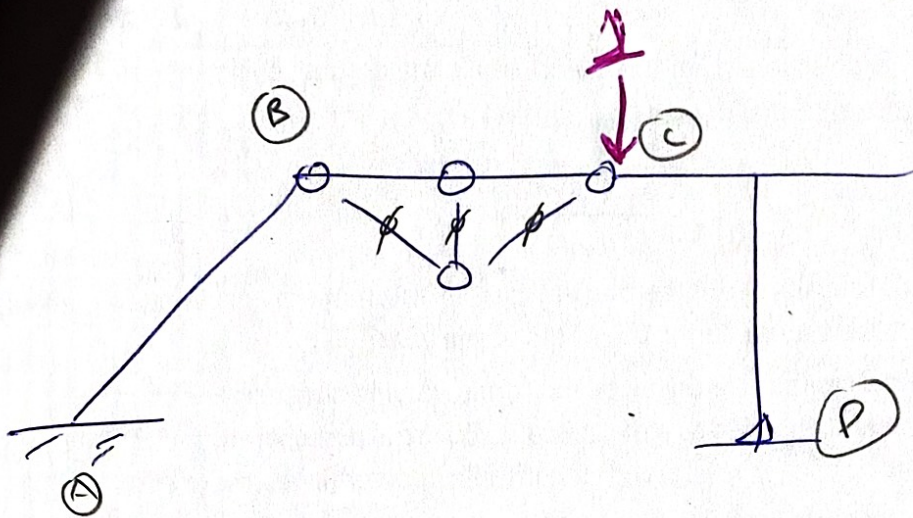
$$180 + 40 = 220$$

$$82 = 82$$

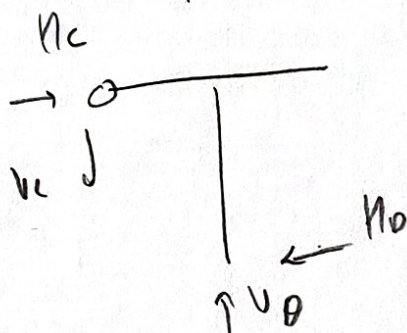


$$Q \times \left(\frac{1}{3} \alpha \times \alpha \right) = - \left(\frac{1}{3} \times 5 \times 200 \times 5,331 \right) = \frac{-1943,7}{100 \times 10^3}$$

$$= 0,0107m$$

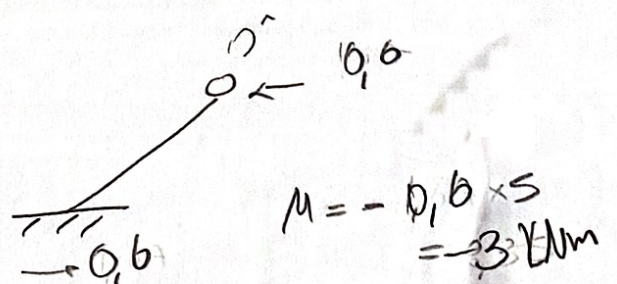
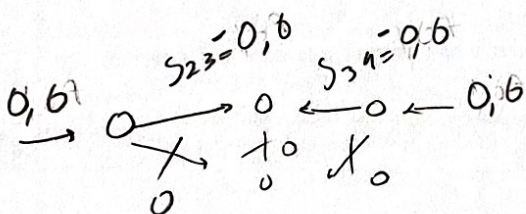


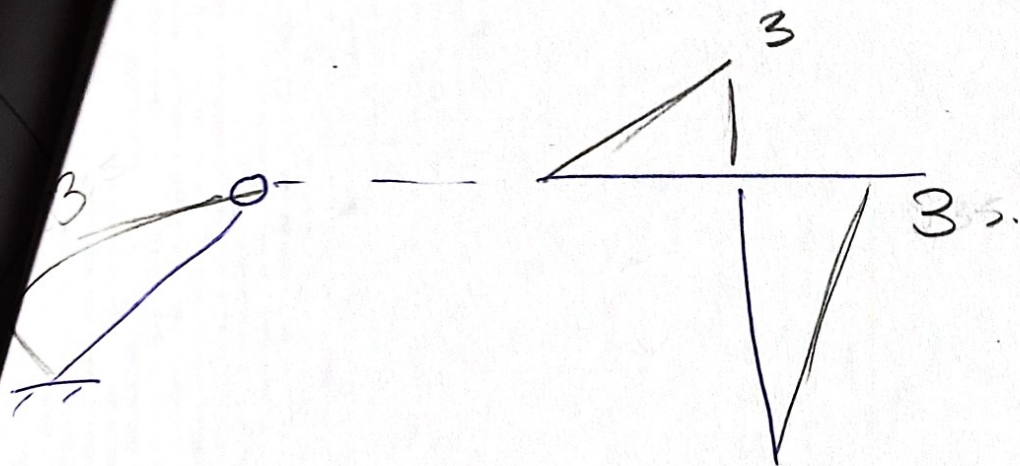
$$\begin{aligned}\sum F_x = 0 &\Rightarrow H_C = H_B \\ \sum F_y = 0 &\Rightarrow V_B + V_C = 1 \\ \sum M_C = 0 &\Rightarrow V_B = 0 \\ V_C &= 1\end{aligned}$$



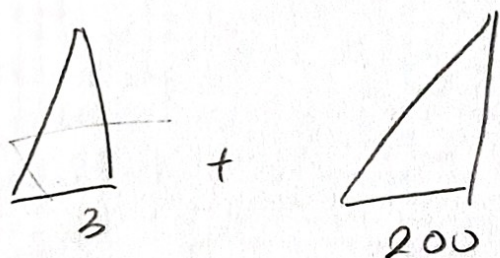
$$\begin{aligned}\sum F_x = 0 &\Rightarrow H_C = H_D \\ \sum F_y = 0 &\Rightarrow V_C = V_D \\ \sum M_C = 0 &\Rightarrow 5H_D = 3V_D \\ V_C = 1 \text{ and } H_C = 0.6 &\Rightarrow V_D = 1\end{aligned}$$

$$\text{At D } H_D = 0.6 \text{ kN} = H_C = H_B$$

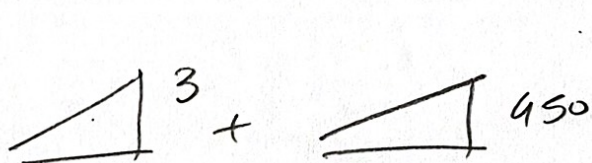




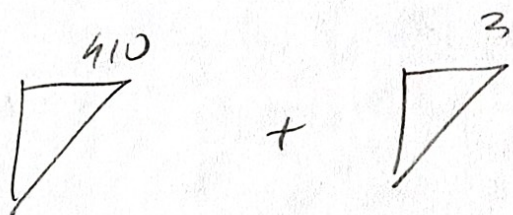
$$\frac{3}{6} \frac{P}{EI} \frac{L^3}{3} \quad \text{or}$$



$$= -\frac{1}{3} \times 200 \times 3 \times 5,831 \quad \text{or} \quad \text{b. k. g. m.}$$



$$= \frac{1}{3} \times 3 \times 450 \times 3 \quad \leftarrow l$$



$$= \frac{1}{3} \times 3 \times 410 \times 5 \quad \leftarrow l$$

$$= \dots$$

$$\frac{5 \pi \bar{N}}{EA} dx = \frac{(0,6 \times 171,95)}{EA} \times 3 \leftarrow l. \quad \frac{EI}{EA} \times 2$$

$$= \dots$$